## MATH1040/7040 Semester 1, 2011

Week 10 Tutorial Solutions

- 1. (a)  $y = e^{7x}$ , which is a graph of exponential growth. Hence the matching graph is Graph K.
  - (b)  $-8y + 9x^2 = -16y + 15x^2$ , so  $8y = 6x^2$ . This equation includes an  $x^2$  term with a positive coefficient, so the graph is a parabola which turns upwards. Also, the *y*-intercept is 0. Hence the matching graph is Graph P.
  - (c) -13y + 9 = -3y 15, so -10y = -24, so  $y = \frac{24}{10}$ . Hence this is a horizontal line, with y positive. Hence the matching graph is Graph C.
  - (d) -8y + 12x = -6y + 14x, so 2y = -2x. Hence this is a straight line, with negative gradient and passing through the origin. Hence the matching graph is Graph I.
  - (e) 3x 13 = -7x + 3, so 10x = 16, so  $x = \frac{16}{10}$ . Hence this is a vertical line, with x positive. Hence the matching graph is Graph B.
  - (f)  $-3y + 9x^2 14 = 6x^2 15$ , so  $3y = 3x^2 + 1$ . This equation includes an  $x^2$  term with a positive coefficient, so the graph is a parabola which turns upwards. Also, the *y*-intercept is positive. Hence the matching graph is Graph O.
  - (g) -2y 2x + 11 = 13y 6x + 11, so 15y = 4x. Hence this is a straight line, with positive gradient and passing through the origin. Hence the matching graph is Graph F.
  - (h)  $y = e^{-3x}$ , which is a graph of exponential decay. Hence the matching graph is Graph L.
- 2. Given an angle a in degrees, to convert a to radians you divide by 180 and multiply by  $\pi$ . Hence the converted angles are:

 $\frac{11\pi}{10} \quad \frac{9\pi}{20} \quad \frac{\pi}{2} \quad -\frac{7\pi}{12} \quad \frac{5\pi}{2} \quad \frac{\pi}{15} \quad -\frac{16\pi}{9} \quad \frac{7\pi}{3}$ 

3. Given an angle a in radians, to convert a to degrees you multiply by 180 and divide by  $\pi$ . Hence the converted angles are:

 $-198^{\circ} - 300^{\circ} 300^{\circ} 126^{\circ} 30^{\circ} 720^{\circ} 1080^{\circ} 468^{\circ}$ 

4. A ladder is placed up against a wall at an angle of elevation of  $30^{\circ}$ . If the ladder is 2m away from the base of the wall, how long is it? How far up the wall does the ladder reach?



Let x be the length of the ladder. Then  $\cos 30^\circ = \frac{2}{x}$ , so  $x = \frac{2}{\cos 30^\circ} \approx 2.31$ m. Let y be the distance the ladder reaches up the wall. Then  $\tan 30^\circ = \frac{y}{2}$ , so  $y = 2\sin 30^\circ \approx 1.15$ m.

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5. (a) The roots of  $y = 4x^2 + 36x$  are the x values that satisfy  $4x^2 + 36x = 0$ . You can solve this equation either by using the quadratic formula or by factoring. Here we will use factoring.

First divide through by 4 to get  $x^2 + 9x = 0$ . Now because  $x^2 + 9x = (x + 9)x$ , the two roots of the quadratic equation are x = -9, 0.

(b) The y-intercept occurs when x = 0, so substituting this into  $y = 4x^2 + 36x$  gives y = 0.

(c)

