

DEPARTMENT OF MATHEMATICS

MATH2000

Triple Integrals in Rectangular Coordinates

- (1) (Stewart ed. 6, p1034, Q9) Evaluate $\iiint_D 2x \, dV$ where $D = \{(x, y, z) \mid 0 \leq y \leq 2, 0 \leq x \leq \sqrt{4 - y^2}, 0 \leq z \leq y\}$
- (2) (Stewart ed. 6, p1034, Q11) Evaluate $\iiint_D 6xy \, dV$ where D lies under the plane $z = 1 + x + y$ and above the region in the x - y plane bounded by the curves $y = \sqrt{x}$, $y = 0$ and $x = 1$.
- (3) (Stewart ed. 6, p1034, Q12) Evaluate $\iiint_D y \, dV$ where D is bounded by the planes $x = 0$, $y = 0$, $z = 0$ and $2x + 2y + z = 4$.
- (4) Evaluate $\iiint_D xz \, dV$ where D is the solid tetrahedron with vertices $(0, 0, 0)$, $(0, 1, 0)$, $(1, 1, 0)$, $(0, 1, 1)$.
- (5) (Stewart ed. 5, p1035, Q36) Write the five other integrals that are equal to the given iterated integral.

$$\int_0^1 \int_0^{x^2} \int_0^y f(x, y, z) \, dz \, dy \, dx.$$