

Lecture 18 Part II: Lecture 10, P.S. 1/1

Similar to (12) & (13) in Lec 10:

$$\sinh(z_1 + z_2) \stackrel{(10), (11), (12)}{=} i \sin(iz_1 + iz_2)$$

$$= -i \sin iz_1 \cos iz_2 - i \cos iz_1 \sin iz_2$$

$$\stackrel{(10), (11), (12)}{=} \sinh z_1 \cosh z_2 + \cosh z_1 \sinh z_2 \quad (A)$$

& similarly ★

$$\cosh(z_1 + z_2) = \cosh z_1 \cosh z_2 + \sinh z_1 \sinh z_2 \quad (B)$$

taking  $z_1 = x$ ,  $z_2 = iy$  leads to

$$\sinh(x + iy) = \sinh x \cosh iy + \cosh x \sinh iy$$

$$\stackrel{(10), (11), (12)}{=} \sinh x \cos y + \cosh x \cdot -i \sin(-y)$$

$$= \sinh x \cos y + i \cosh x \sin y \quad (C)$$

similarly ★

$$\cosh(x + iy) = \cosh x \cos y + i \sinh x \sin y \quad (D)$$