

LECTURE 18 part I: revision for mid-sem ^{1/2}

* $z = x + iy = (x, y)$
" "
 $re^{i\theta}$

* $\mathbb{C}$ as a field (not ordered, can't be ordered)

* Arg vs $\arg$ (vs $\mathbb{Q}\arg$)

* $e^{i\theta} = \cos\theta + i\sin\theta$

* $e^{in\theta} = \cos n\theta + i\sin n\theta$

* n th roots

* quadratic formula

* F^n 's as mappings (linear, $1/z$)

* Möbius transformations

In partic $\begin{Bmatrix} \text{circles} \\ \text{lines} \end{Bmatrix} \rightarrow \begin{Bmatrix} \text{circles} \\ \text{lines} \end{Bmatrix}$

* Riemann sphere

* $\bar{\mathbb{C}}$, Möbius transformations: $\bar{\mathbb{C}} \rightarrow \bar{\mathbb{C}}$

* inverse F^n 's (inv of $\exp$?)

* Log vs Log (vs Log).

* branch, branch cut.

* trig & hyperbolic F^n 's (inverses, zeros, identities).

* bounded & unbounded F^n 's & sets.

* basic topology on $\bar{\mathbb{C}}$ (& on $\bar{\mathbb{C}}$)

* limits (including ∞)

continuity, differentiability.

Cauchy-Riemann eq's $\left\{ \begin{array}{l} * \text{rectangular} \\ * \text{polar} \\ * \text{(Wirtinger)} \end{array} \right.$

* CR as necessary cond's for $\mathbb{C}$ -diff'ability

* Sufficient cond's for $\mathbb{C}$ -diff'ability

* Analytic f's

* Analytic vs diff'ble

(real analytic vs smooth f's in $\mathbb{R}^n$:)
not examinable in mid-sem.