

In Semester Examination, 14 April, 2026

MATH3401/MATH3901**Complex Analysis/Advanced Complex Analysis**
(2 Unit Course)**Time:** 15 minutes for scanning/download/upload, 50 Minutes for working

No perusal time before examination begins

CREDIT WILL BE GIVEN ONLY FOR WORK WRITTEN ON THIS EXAMINATION SCRIPT.

FULL WORKING MUST BE SHOWN.

Use the back pages if the space provided is insufficient, and/or for rough working.

Answer **all** questions. Show all working. Questions carry the marks indicated.

Credit will only be given for work written on this examination paper. Total marks are 100.

This examination paper has 10 printed pages.

Calculators - Casio FX82 series or UQ approved (labelled) only.

One A4 page (single sided) of hand-written notes permitted.

By uploading your completed exam, you are confirming that you complied with the University's academic integrity guidelines in completing this exam, that all work is your own, that you obtained no assistance directly or indirectly from any source other than those listed as permitted.

FAMILY NAME (PRINT): _____

GIVEN NAMES (PRINT): _____

STUDENT NUMBER:

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SIGNATURE: _____

| EXAMINER'S USE ONLY | | | |
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| QUESTION | MARK | QUESTION | MARK |
| 1 | | 3 | |
| 2 | | 4 | |
| TOTAL MARKS | | | |

**MATH3401/MATH3901 — Complex Analysis/Advanced Complex Analysis
In Semester Examination, 14 April, 2026 (continued)**

1. (a) **[12 marks]** Find all solutions of the equation $z^2 - 3iz - 2 = 0$. Express your answers in the form $x + iy$, with $x, y \in \mathbb{R}$.
(b) **[13 marks]** Find all solutions of the equation $z^4 - 3iz^2 - 2 = 0$. Again, express your answers in the form $x + iy$, with $x, y \in \mathbb{R}$.

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(Question 1 continued).

**MATH3401/MATH3901 — Complex Analysis/Advanced Complex Analysis
In Semester Examination, 14 April, 2026 (continued)**

2. (a) [15 marks] Prove that $\tan^{-1} z = \frac{i}{2} \log \left(\frac{i+z}{i-z} \right)$, noting any restrictions on your domain.
- (b) [10 marks] Find all solutions $z \in \mathbb{C}$ of $\tan z = 1$ (express them in the form $x + iy$).

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(Question 2 continued).

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In Semester Examination, 14 April, 2026 (continued)

3. (a) [15 marks] For $z = x + yi \in \mathbb{C}$, let $f(z) = x^2 + y^3i$.

(i) Find all points $z \in \mathbb{C}$ at which f satisfies the Cauchy-Riemann equations. (Hint: the set is non-empty).

(ii) Find all points $z \in \mathbb{C}$ at which f is differentiable (Hint: the set is non-empty). Make sure you justify your answer.

(iii) Show that f is nowhere analytic in \mathbb{C} .

(iv) Explain why there is no contradiction between your answers to (ii) and (iii).

Explain your answers. Note: no marks will be given for an answer without explanation, even if it is correct.

(b) [10 marks] Calculate $\frac{d}{dz}(1+i)^z$, explaining any restrictions you need to make for your answer to be valid.

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(Question 3 continued).

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4. (a) [**18 marks**] Determine the Möbius transformation (viewed as a mapping on $\overline{\mathbb{C}}$) mapping 2 to 0, i to ∞ , and 0 to $-2i$.
- (b) [**7 marks**] Determine the Möbius transformation mapping 2 to 0, $5i$ to i , and $1 + i$ to i , or explain why no such Möbius transformation exists.

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extra working space

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bonus extra working space